

Maths
Specimen

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Year 21-22

# Chapter-6 Be My Multiple, I'll Be Your Factor 



> Key Points to Remember

- Introduction.
- Highest common factor by prime factorization method
- Lowest common factor by prime factorization method
- Make the factor tree by prime factorization method
- Activity.


## Introduction.

- Fractor - A number is said to be a factor of another number if it can divide the number completely.

Example $-6 \div 3=2$

- 1 is the factor of every number. It is also the smaller factor of a number.
- Multiples - A number is said to be a multiple of another number if it can be divided completely by that number.
Example - 2 can divide 4 completely. So, 4 is a multiple of 2 .

- Prime numbers - The numbers having only two factors - 1 and the number itself are called prime numbers.
Example -

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :--- | :--- | :--- | :--- | :--- |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

- Composite numbers - The numbers having more than two factors are called composite numbers.

Example - 4, 6, 8, 9, 10, $12 \ldots .$.

- 1 is either a prime or a composite number.


## Highest common factor (H.C.F.)

While doing prime factorization by division method, start dividing the given number by the smallest prime number and continue till we are left with 1 .

1. 8 and 12

| 2 | 8 |
| :--- | :--- |
| 2 | 4 |
| 2 | 2 |
|  | 1 |


| 2 | 12 |
| :--- | :--- |
| 2 | 6 |
| 3 | 3 |
|  | 1 |

$8=2 \times 2 \times 2$
$12=2 \times 2 \times 3$
H.C.F $=2 \times 2=4$

Thus, H.C.F. of 8 and 12 is 4
2. 10 and 25

$10=2 \times 5$
$25=5 \times 5$
H.C.F. $=5$

Thus, H.C.F. of 10 and 25 is 5.
3. 10,15 and 55

$10=2 \times 5$
$15=3 \times 5$
$55=5 \times 11$
H.C.F. $=5$

Thus, H.C.F. of 10,15 and 55 is 5.
4. 200,120 and 240

| 2 | 200 |
| :--- | :--- |
| 2 | 100 |
| 2 | 50 |
| 5 | 25 |
| 5 | 5 |
|  | 1 |


| 2 | 120 |
| :---: | :---: |
| 2 | 60 |
| 2 | 30 |
| 3 | 15 |
| 5 | 5 |
|  | 1 |


| 2 | 240 |
| :---: | :---: |
| 2 | 120 |
| 2 | 60 |
| 2 | 30 |
| 3 | 15 |
| 5 | 5 |
|  | 1 |

$$
200=2 \times 2 \times 2 \times 5 \times 5
$$

$$
120=2 \times 2 \times 2 \times 3 \times 5
$$

$$
240=2 \times 2 \times 2 \times 2 \times 3 \times 5
$$

H.C.F. $=2 \times 2 \times 2 \times 5$

Thus, H.C.F. of 200, 120 and 240 is 40 .
5. 35,105 and 140

$35=5 \times 7$
$105=3 \times 5 \times 7$
$140=2 \times 2 \times 5 \times 7$
H.C.F. $=5 \times 7$

Thus, H.C.F. of 35, 105 and 140 is 35.

* Lowest common multiple. (L.C.M.)

1. 6,8 and 12 .

| 2 | 6, | 8, | 12 |
| :---: | :---: | :---: | :---: |
| 2 | 3, | 4, | 6 |
| 2 | 3, | 2, | 3 |
| 3 | 3, | 1, | 3 |
|  | 1, | 1, | 1 |

L.C.M $=2 \times 2 \times 2 \times 3$

Thus, L.C.M of 6,8 and 12 is 24 .
2. 24 and 30

| 2 | $\underline{24}$ | $\underline{30}$ |
| :--- | :---: | :---: |
| 2 | $\underline{12}$ | $\underline{15}$ |
| 2 | $\underline{6}$ | $\underline{15}$ |
| 3 | $\underline{3}$ | $\underline{15}$ |
| 5 | 1 | $\underline{5}$ |
|  | 1 | 1 |

L.C.M $=2 \times 2 \times 2 \times 3 \times 5=120$

Thus, L.C.M. of 24 and 30 is 120 .
3. 60 and 282

| $\mathbf{2}$ | $\mathbf{6 0}$ | $\mathbf{2 8 2}$ |
| :---: | :---: | :---: |
| $\mathbf{2}$ | 30 | 141 |
| $\mathbf{3}$ | 15 | 141 |
| $\mathbf{5}$ | 5 | 47 |
| $\mathbf{4 7}$ | 1 | 47 |
|  | 1 | 1 |

L.C.M $=2 \times 2 \times 3 \times 5 \times 47=2820$

Thus, L.C.M. of 60 and 282 is 2820.
4. 102,119 and 153

| 2 | $102,119,153$ |
| :---: | :--- |
| 3 | $51,119,153$ |
| 3 | $17,119,51$ |
| 7 | $17,119,17$ |
| 17 | $17,17,17$ |
|  | 111 |

L.C.M $=2 \times 3 \times 3 \times 7 \times 17=2142$

Thus, L.C.M. of 102, 119 and 153 is 2142.
5. 36,48 and 72

| 2 | 36, | 48, | 72, |
| :--- | :--- | :--- | :--- |
| 2 | 18, | 24, | 36 |
| 2 | 9, | 12, | 18 |
| 2 | 9, | 6, | 9 |
| 3 | 9, | 3, | 9 |
| 3 | 3, | 1, | 3 |
|  | 1, | 1, | 1 |

L.C.M $=2 \times 2 \times 2 \times 2 \times 3 \times 3=144$

Thus, L.C.M. of 36,48 and 72 is 144 .

* Make the factor tree.

1. 32


Factors of $32=2 \times 2 \times 2 \times 2 \times 2$
2. 48


Factors of $48=2 \times 2 \times 2 \times 2 \times 3$
3. 100


Factors of $100=2 \times 2 \times 5 \times 5$
4. 72


Factors of $72=1 \times 2 \times 2 \times 2 \times 3 \times 3$.
5. 225


Factors of $225=3 \times 3 \times 5 \times 5$
6. 45


Factors of $45=3 \times 3 \times 5$

## Word problems:

1. There are three buckets containing $24 \mathrm{~L}, 36 \mathrm{~L}$ and 48 L of milk. Find the capacity of smallest bucket that can measure the milk in the three buckets.

## Solution -

The capacity of the smallest required bucket will be the L.C.M. of 24,36 and 48 . So we find the L.C.M.

| 2 | $24,36,48$ |  |  |
| :--- | :---: | :---: | :---: |
| 2 | $12,18,24$ |  |  |
| 3 | $6,9,12$ |  |  |
| 2 | 2, | 4 |  |
| 2 | 1, | 3, | 1 |

L.C.M. $=2 \times 2 \times 2 \times 2 \times 3 \times 3=144$

Thus L.c.m of 24,36 and 48 is 144 .
2. Three plastic containers contain $400 \mathrm{~L}, 500 \mathrm{~L}$ and 600 L of oil. Find the capacity of the largest container that can be filled an exact number of times from each drum.

## Solution -

The capacity of the largest required container will be the H.C.F. of 400,500 and 600 . So we find the H.C.F.

$400=2 \times 2 \times 2 \times 2 \times 5$
$500=2 \times 2 \times 5 \times 5 \times 5$
$600=2 \times 2 \times 2 \times 3 \times 5 \times 5$
H.C.F. is $2 \times 2 \times 5=20$

So, the capacity of required container is 20 L .

## Activity

* Make venn diagram of common multiples:

For example (text book page no 92)


## Chapter - 7 Can You See the Pattern?

## Key Points To Remember

- Complete the pattern
- Numbers and numbers.
- MagicHexagon
- Magic square
- Activity
* Complete the pattern.(Do it in text book page no 100 and 101)


Answer

e)


The rule of the pattern is - turning by $45^{\circ}$ each time. Which will be the next? Tick $(\checkmark)$ the right one.


Using the same rule take it forward till you get back to what you started with.
f)

g)


## Answer.

f)

g)
ค


## * Numbers and numbers.( Do it in text book page no 105)

## - Fill in the blanks:

1. $24+\underline{\mathbf{1 9}}+37=37+24+19$
2. $215+120+600=600+\underline{\mathbf{2 1 5}}+120$
3. $14+\underline{\mathbf{3 4}}+\underline{\mathbf{2 0}}=34+14+20$
4. $\underline{\mathbf{8 0}}+42+\underline{\mathbf{6 5}}=65+\underline{\mathbf{4 2}}+80$
5. $200+300+\underline{\mathbf{4 0 0}}=\underline{\mathbf{2 0 0}}+\underline{\mathbf{3 0 0}}+400$
6. $48 \times 13=13 \times \underline{48}$
7. $\underline{\mathbf{6 4}} \times 55=55 \times 64$
8. $255 \times 15 \times 4=\mathbf{1 5} \times \mathbf{2 5 5} \times 4$
9. $14 \times \underline{\mathbf{7 0}} \times 5=14 \times 5 \times 70$

## * MagicHexagon.



Solution -
$108 \div 9=12$
$12 \times 7=84$
$7 \times 17=119$
$17 \times 6=102$
$6 \times 11=66$
$11 \times 9=99$

b)

## Solution -

$104 \div 8=13$

$$
78 \div 13=6
$$

$$
6 \times 4=24
$$

$$
64 \div 4=16
$$

$$
16 \times 8=128
$$

$$
8 \times 8=64
$$


c)

Solution -
$10 \times 2=20$
$2 \times 13=26$
$13 \times 5=65$
$5 \times 14=70$
$84 \div 14=6$
$6 \times 10=60$


## * Magicsquare

1. Fill this square using all the numbers from 46 to 54 . Rule: The total of each line is 150 .

|  |  | 49 |
| :--- | :--- | :--- |
| 46 |  |  |
|  | 52 | 47 |

Solution -
$150-(49+47)=54$
$150-(52+47)=51$
$150-(51+46)=53$
$150-(53+49)=48$
$150-(48+52)=50$

| 53 | 48 | 49 |
| :---: | :---: | :---: |
| 46 | 50 | 54 |


| 51 | 52 | 47 |
| :--- | :--- | :--- |

2. Fill this square using all the numbers from 6 to 14 . Rule: The total of each line is 30 .

| 13 |  | 11 |
| :--- | :--- | :--- |
|  |  | 7 |
|  | 10 |  |

## Solution -

$$
\begin{aligned}
& 30-(11+7)=12 \\
& 30-(12+10)=8 \\
& 30-(8+13)=9 \\
& 30-(13+11)=6 \\
& 30-(6+10)=14
\end{aligned}
$$

| 13 | 6 | 11 |
| :---: | :---: | :---: |
| 9 | 14 | 7 |
| 8 | 10 | 12 |

3. Fill this square using all the numbers from 21 to 29 .

Rule: The total of each line is 75 .

|  |  | 28 |
| :--- | :---: | :---: |
|  | 25 |  |
| 22 | 27 |  |

## Solution -

$75-(25+27)=23$
$75-(23+28)=24$
$75-(24+22)=29$
$75-(29+25)=21$
$75-(28+21)=26$

| 24 | 23 | 28 |
| :---: | :---: | :---: |
| 29 | 25 | 21 |
| 22 | 27 | 26 |

* Activity (Do it in text book page no 111)

For Example -

b) T Take a number 9

c)

NTake a number $\square$


TAgain double it
WAdd the number you took
first to the answer Now again double it


WDivide by 10


